

Deep Learning with TensorFlow

http://cvml.ist.ac.at/courses/DLWT_W18

Lecture 5: Convolutional Networks

Convolutional Neural Networks

Martin Töpfer

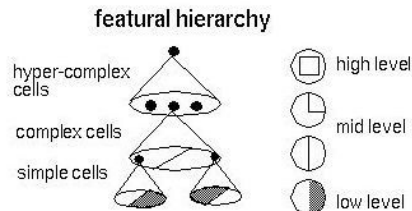
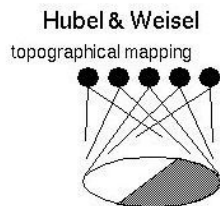
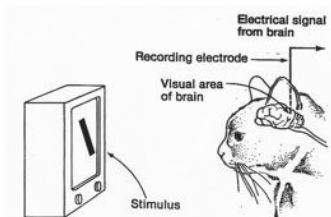
IST Austria

December 17, 2018

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- 3 Pooling Layer
- 4 CNN Architecture

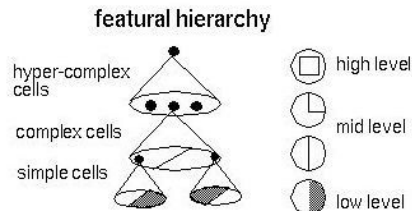
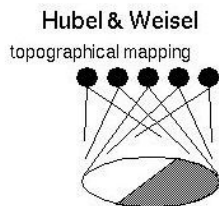
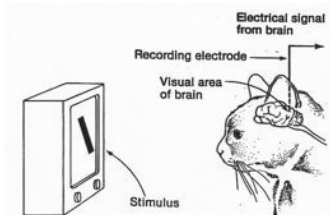
Biological motivation

- 1958: David Hubel, Torsten Weisel: neurons in visual cortex have often small **local receptive field**
 - some reacts only to certain shapes



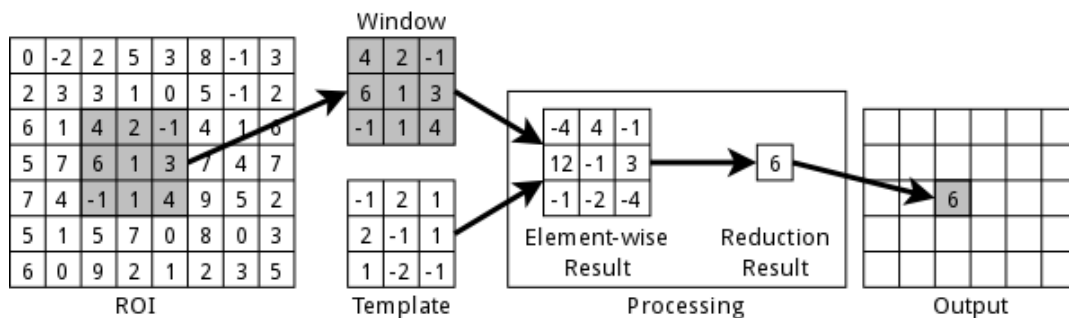
Biological motivation

- 1958: David Hubel, Torsten Weisel: neurons in visual cortex have often small **local receptive field**
 - some reacts only to certain shapes
- Some neurons have **larger receptive field**
 - they recognize more complex patterns
 - combines outputs of lower-level neurons



Computer graphics motivation - filters

- for capturing **features** of an image like edge detection etc.
- multiply each pixel and its neighbours by some matrix

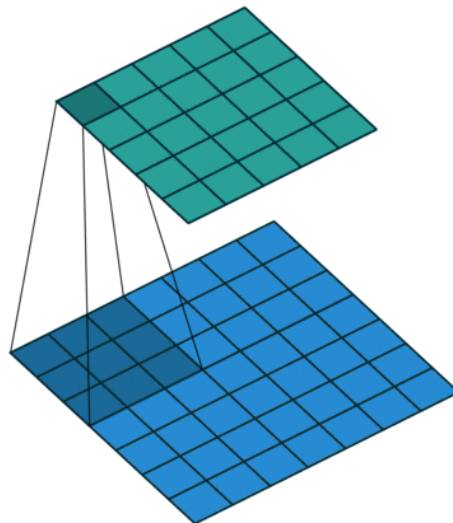


ML motivation - fully-connected networks disadvantages

- not using **structure** of the input data
 - 2D picture treated as 1D vector
- a lot of **parameters** to learn
 - especially for larger input
- **locality**
 - pattern recognized on a particular place is not recognized elsewhere

Convolutional Layer

- Each neuron is connect only to its **receptive field** = small rectangle in previous layer

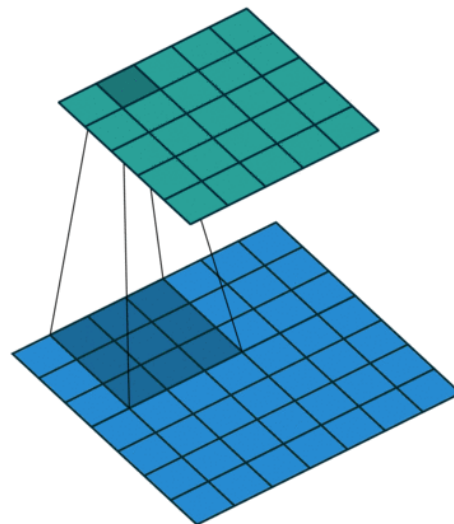


http://www.cvc.uab.es/people/joans/slides_tensorflow/tensorflow_html/layers.html

<http://index-of.es/Varios2/HandsonMachineLearningwithScikitLearnandTensorflow.pdf>

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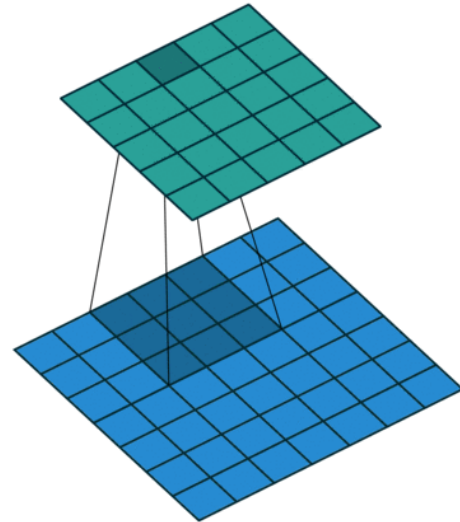


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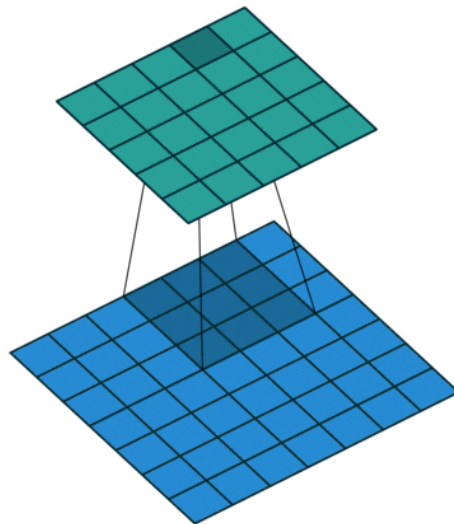


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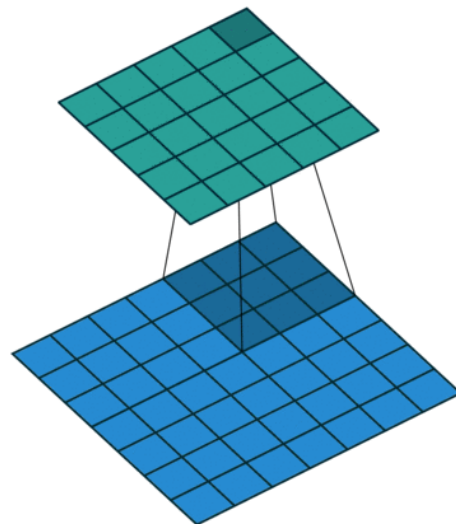


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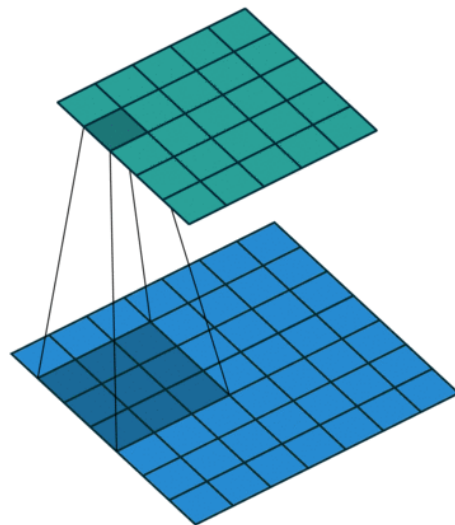


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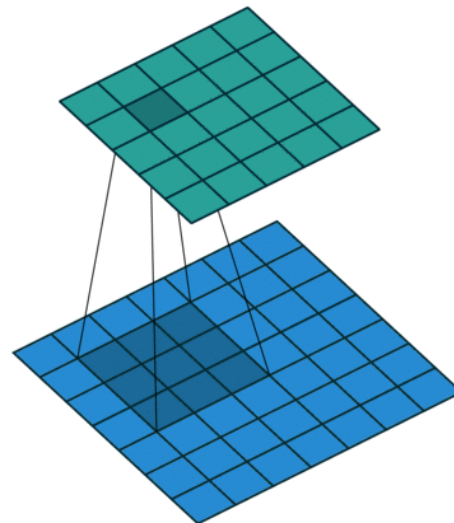


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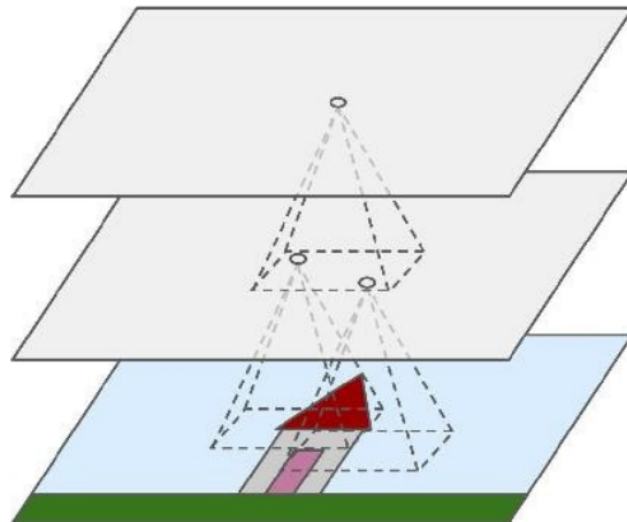


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Convolutional Layer

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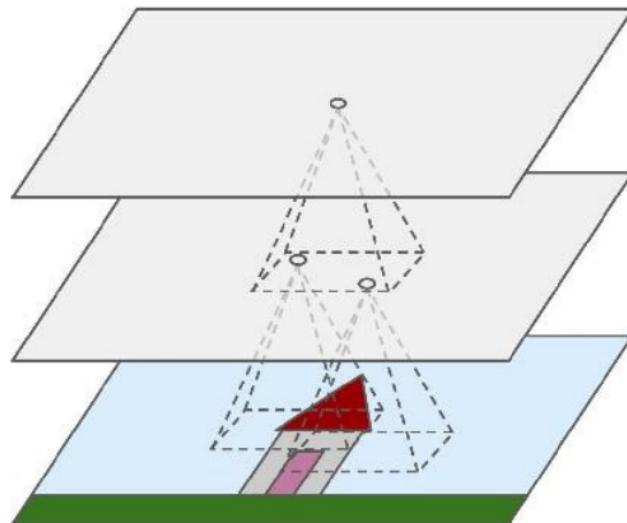


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Convolutional Layer

- Each neuron is connect only to its **receptive field** = small rectangle in previous layer
- 1st layer: low-level features

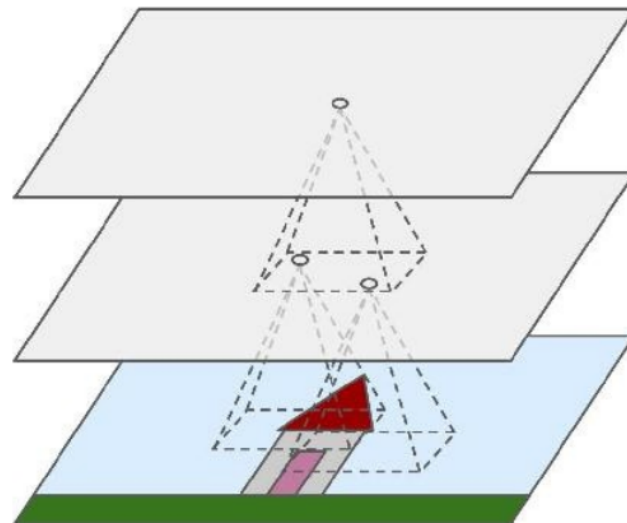


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Convolutional Layer

- Each neuron is connect only to its **receptive field** = small rectangle in previous layer
- 1st layer: low-level features
- 2nd layer: higher-level features
- ...

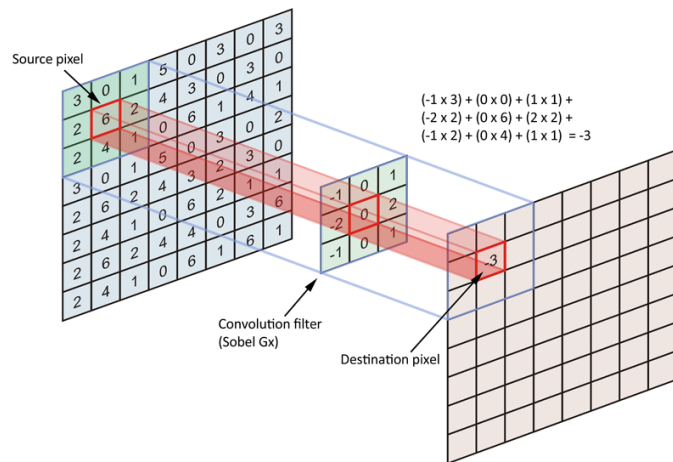


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What does neuron do?

- each neuron outputs multiplication of its reception field by a matrix = **filter**
 - followed by activation function (oftenly ReLU)
- the same filter for all neurons
- filters are learned
- **feature map**



$$z_{i,j} = a \left(b_k + \sum_{u=0}^{w_k} \sum_{v=0}^{h_k} x_{i+u,j+v} \cdot w_{u,v} \right)$$

$z_{i,j}$ = output of filter in position i, j ; w_k, h_k = width and height of the filter;
 $w_{u,v}$ = weights of filter; $x_{i,j}$ = input from previous layer in position i, j ;
 b_k = bias term; a = activation function

Stacking feature maps

- more filters in each conv. layer
- filter uses all feature maps from previous layer

$z_{i,j,k}$ = output of a filter k in position i,j

w_k, h_k = width and height of the filter

n_{l-1} = num. of f. maps in previous layer

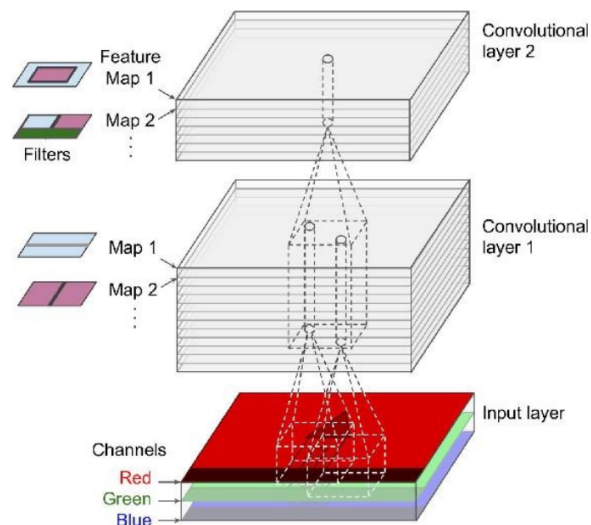
$w_{u,v,k',k}$ = weights of filter k

$x_{i,j,k'}$ = output of a filter k' from previous layer in position i,j

b_k = bias of filter k

a = activation function

$$z_{i,j,k} = a \left(b_k + \sum_{u=0}^{w_k} \sum_{v=0}^{h_k} \sum_{k'=0}^{n_{l-1}} x_{i+u,j+v,k'} \cdot w_{u,v,k',k} \right)$$

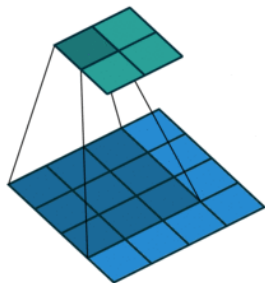


Padding

How to behave on the border?

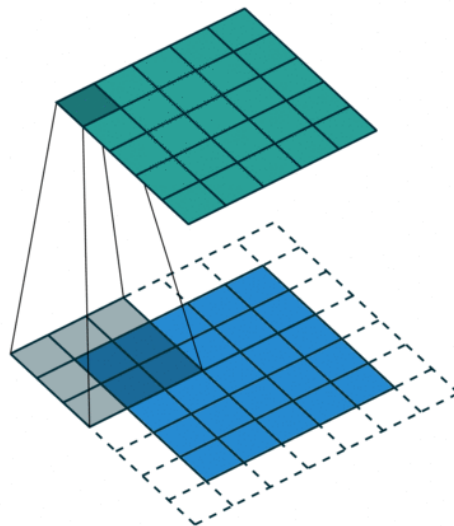
VALID

- new layer slightly smaller
- less common



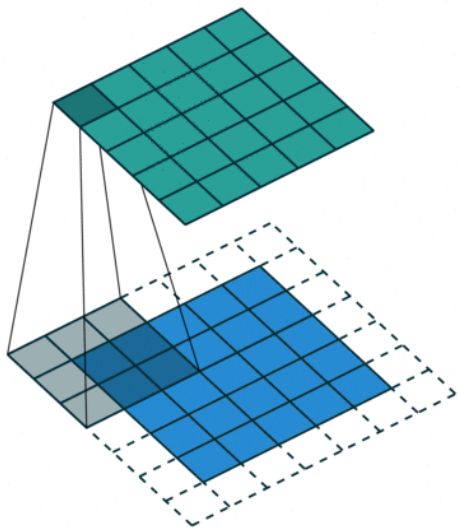
SAME

- new layer of the same size
- add zeros around

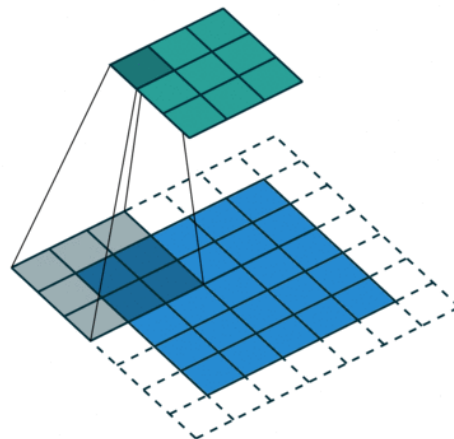


Strides

strides = [1, 1, 1, 1]

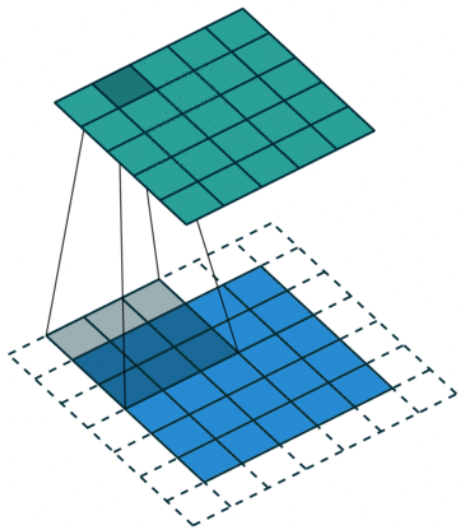


strides = [1, 2, 2, 1]

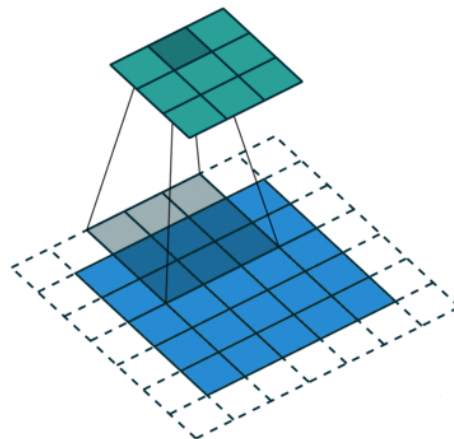


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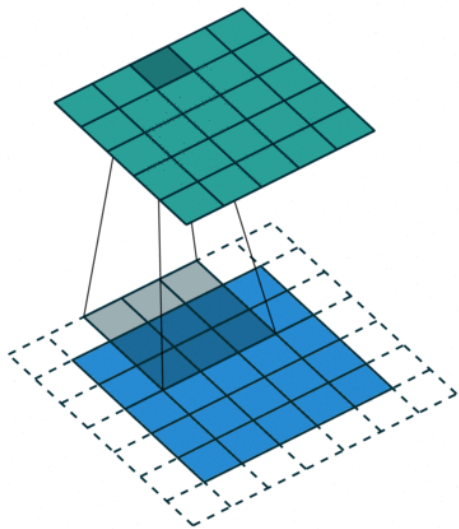


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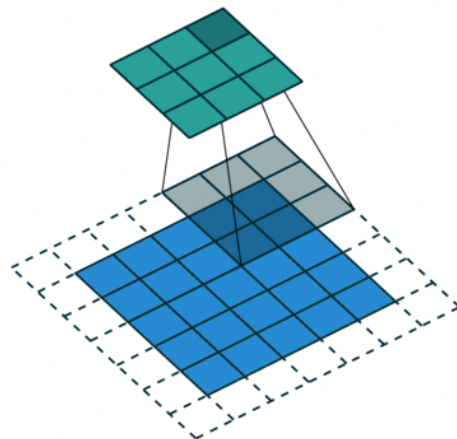


Strides

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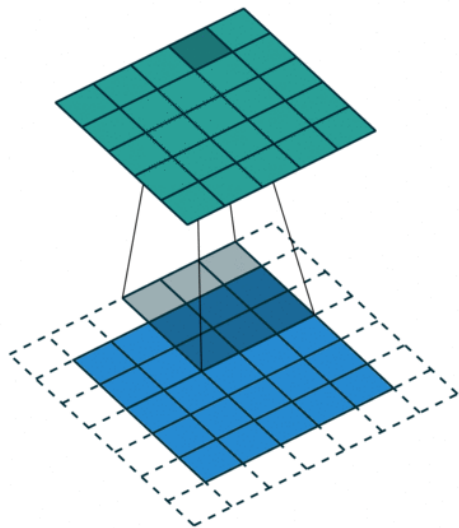


strides = [1, 2, 2, 1]

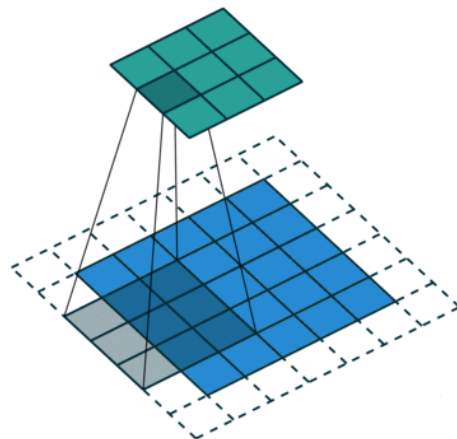


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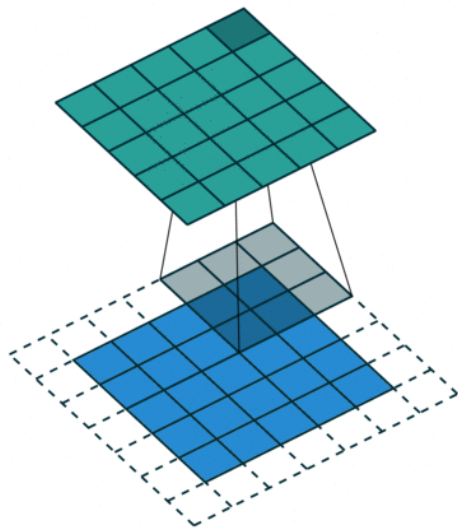


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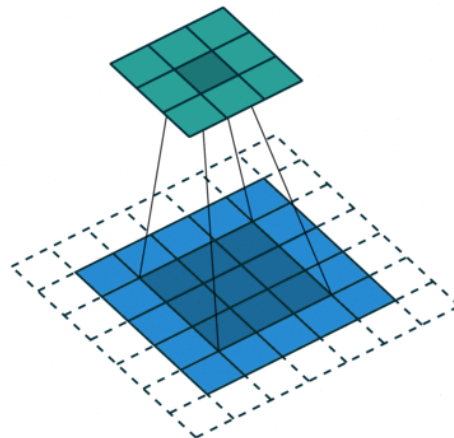


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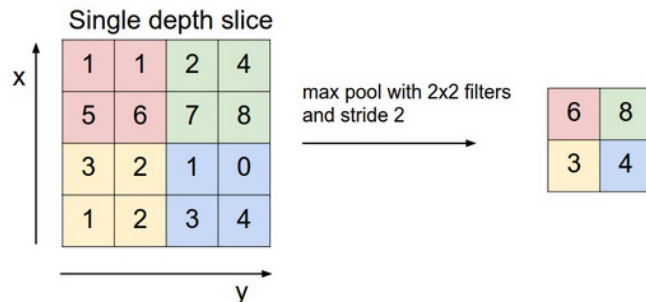
Convolutional Layer - Tensorflow overview

```
c_filters = 32    # number of filters
c_kernel_size = 3  # for square kernel 3x3
c_strides = [1,2,2,1]  # [mini-batch size, height,
                        width, depth in feature maps]
c_pad = "SAME"    # SAME or VALID
c_act = tf.nn.relu  # activation function

conv_layer = tf.layers.conv2d(previous_layer,
                               kernel_size = c_kernel_size, strides = c_strides,
                               padding = c_pad, activation = c_act)
```

Pooling layer

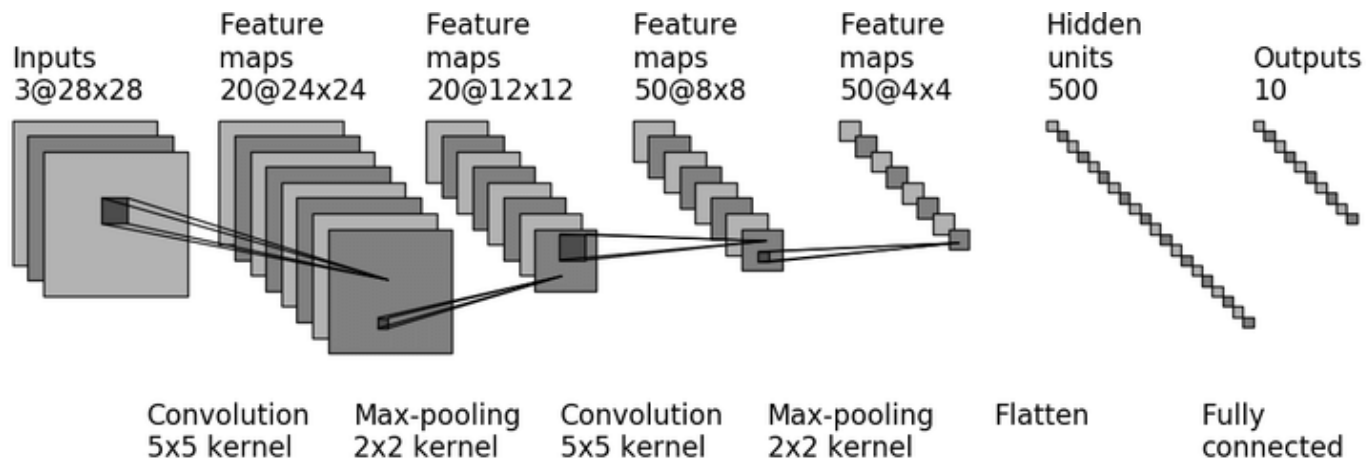
- **shrinking image** - either taking maximum or average
- reduction of computational load (memory)
- reduction of parameters (overfitting)



```
pool_layer = tf.nn.max_pool(input_layer ,  
                             ksize=[1, 2, 2, 1],  
                             strides=[1, 2, 2, 1],  
                             padding="VALID")
```

CNN Architecture

Le-Net5 (1998):



https://www.researchgate.net/publication/312170477_On_Classification_of_Distorted_Images_with_Deep_Convolutional_Neural_Networks

CNN compared to fully-connected networks

- **smaller** number of parameters (filters need a lot of memory but they share parameters)
- better results than fully-connected networks
- **much more** hyperparameters (different architectures + hyperparameters for each convolutional layer)